

# Evaluation and Analysis of Influence from Other Radio Systems in Wideband Non-Contiguous OFDM Receiver

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Advanced Telecommunications Research Institute International (ATR)

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# Introduction

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We are making progress of research for

## Wideband Non-Contiguous OFDM

- Allocates subcarriers (SCs) onto many dispersed idle bands,
- Aggregates, Obtains high data traffic.

Previous Paper :

Evaluate influence of interference from other radio systems  
(the Most Serious Issue in WNC-OFDM system)

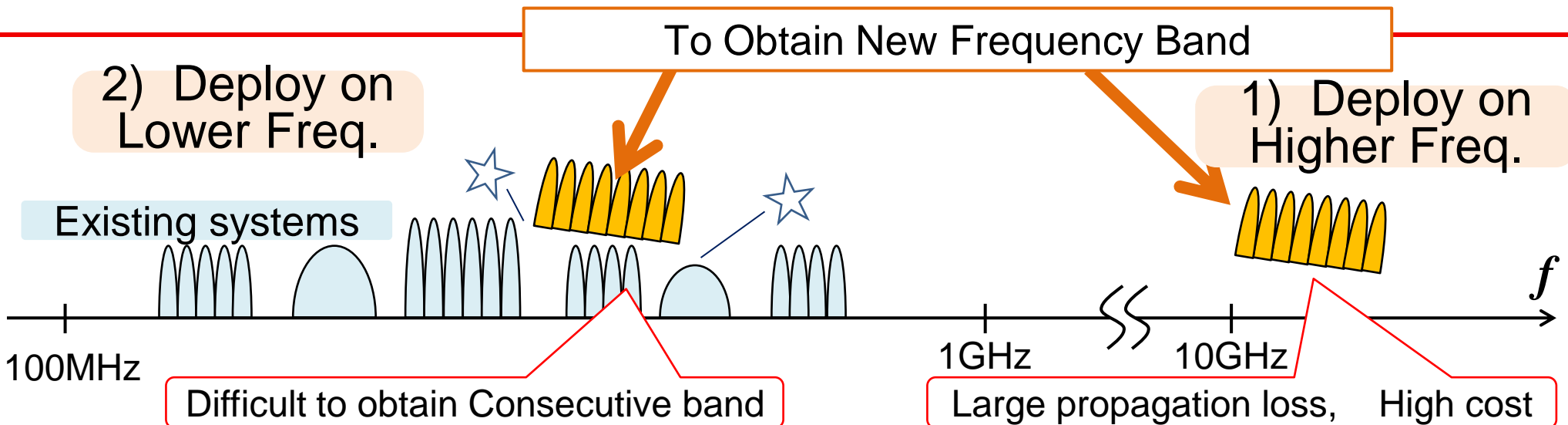
BER were quite different from Gaussian noise environment.



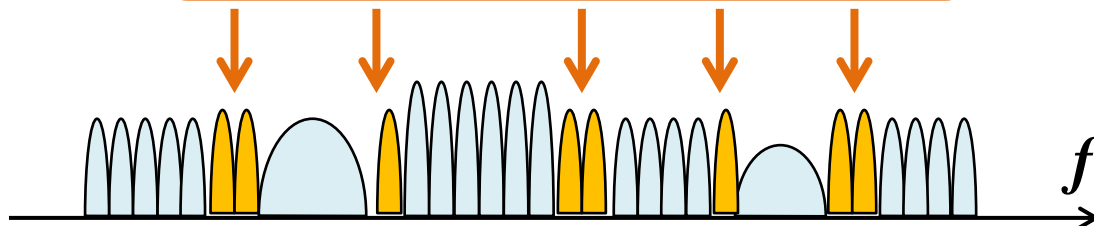
This Paper conducts :

conducts Theoretical analysis in order to Confirm validity of the interference characters observed in the previous evaluation.

# Overview of WNC-OFDM



Allocate Subcarriers onto many dispersed idle bands



Aggregate, obtain high data traffic

## WNC-OFDM

Wideband Non-Contiguous OFDM

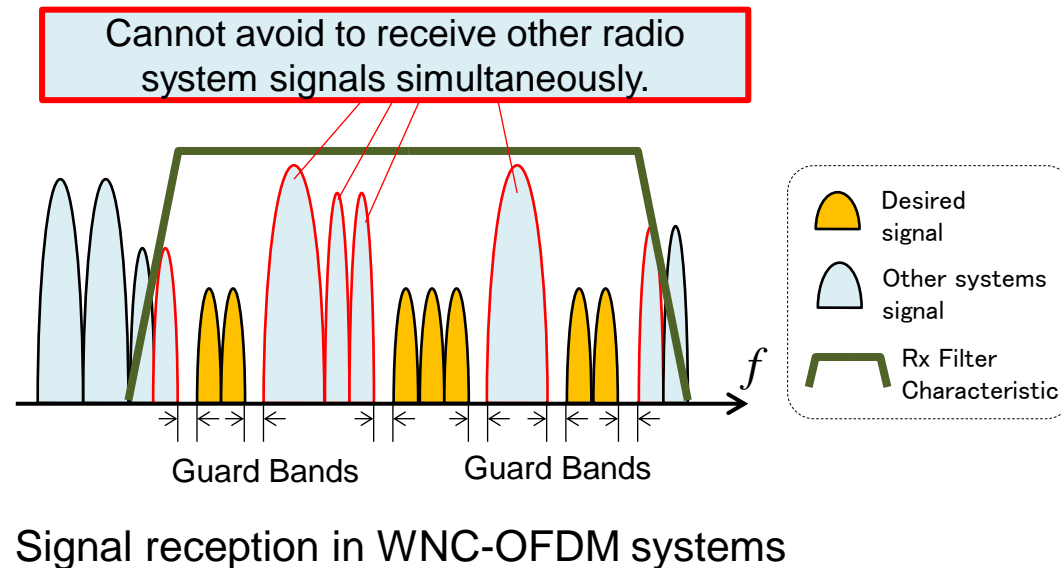
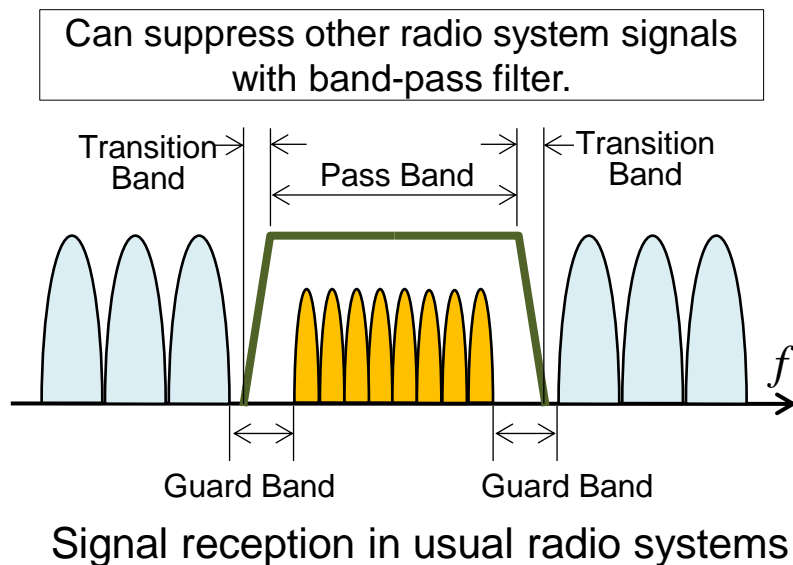
Supports **Extremely Wide Band**  
(170MHz ~ 1GHz)

→ Advantageous to gather  
dispersed idle bands

# Interference from other systems signal

RF-units **cannot be implemented independently** for each dispersed SC block. Required to Cover some SC blocks together with a RF-unit of wider bandwidth.

→ **Cannot avoid to receive other radio systems signal simultaneously.** (WNC-OFDM's characteristic difficulty)



Important to **comprehend** the influence of interference from other radio systems and tolerance for the interference

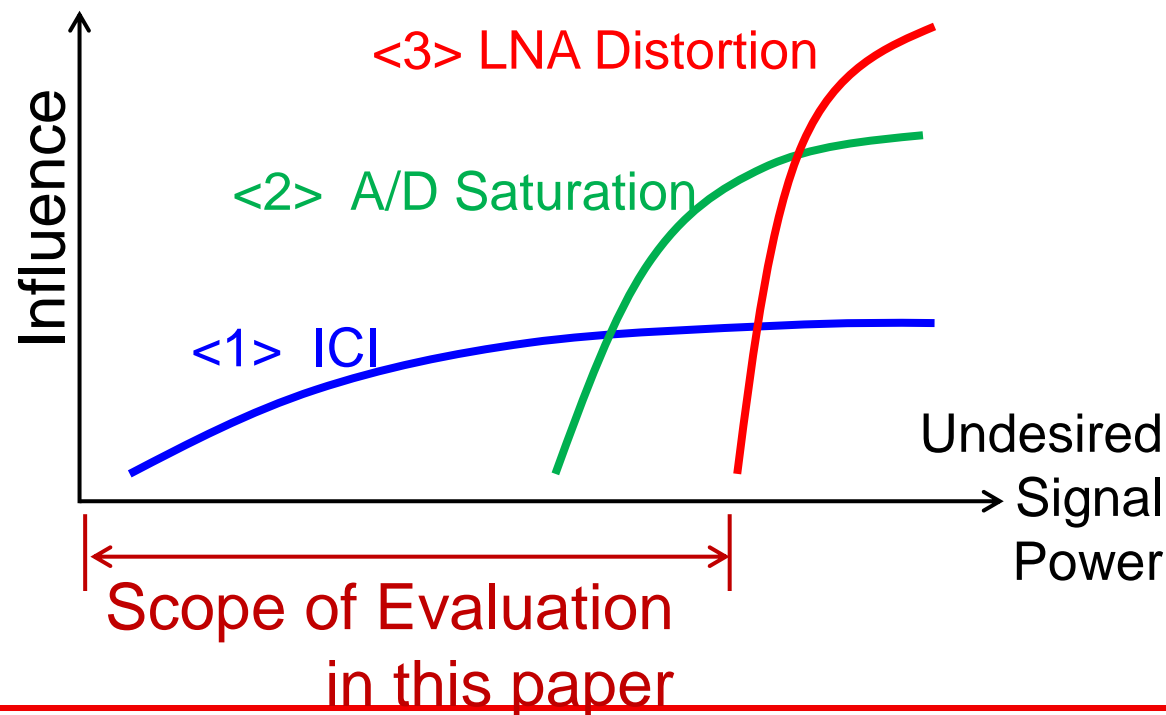
# Interference from other systems signal

Issues caused by simultaneous reception of large undesired signals

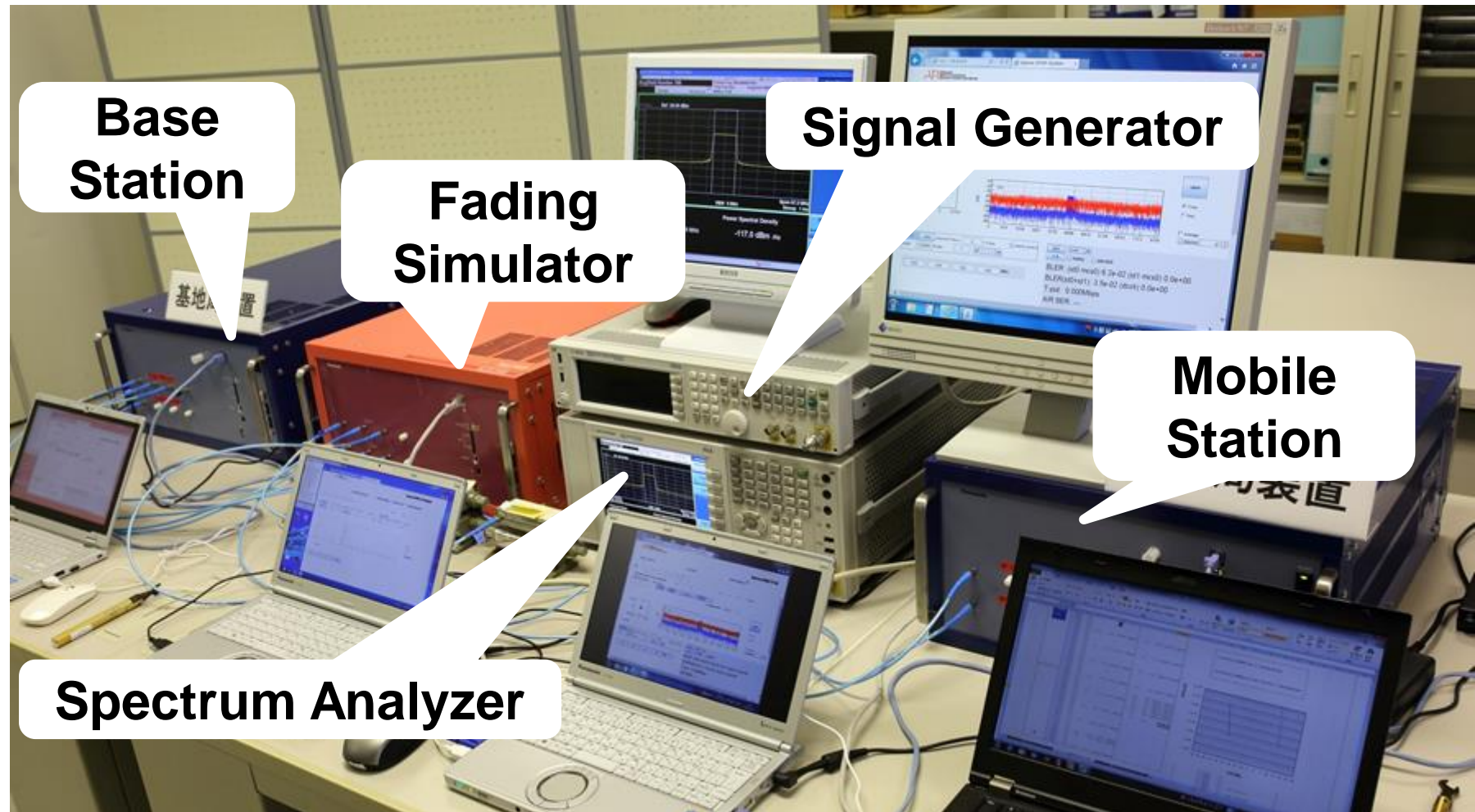
<1> Collapse of Orthogonality at FFT ( → ICI)

<2> Saturation at A/D converter

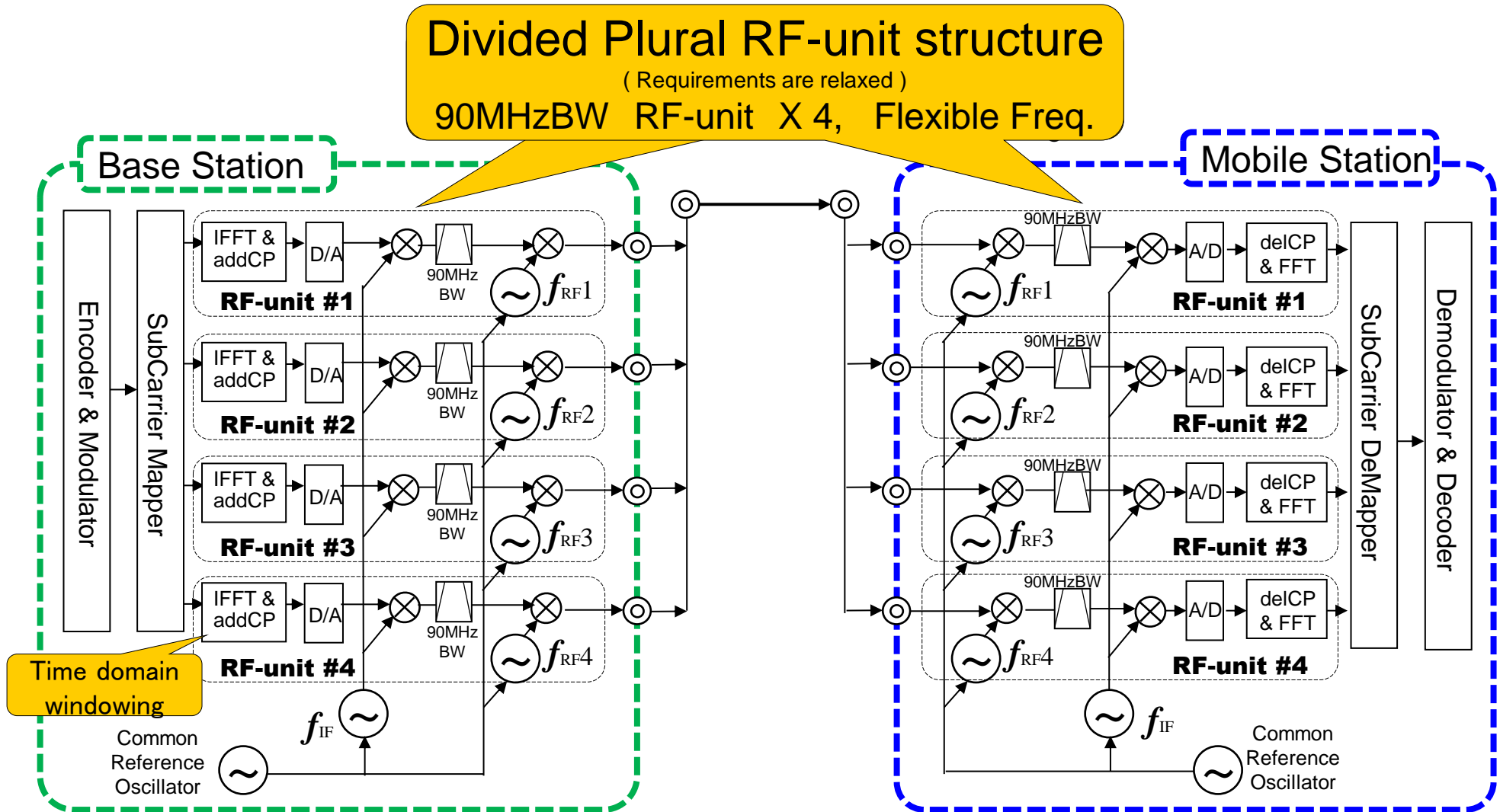
<3> Nonlinear Distortion at frontend LNA



# External view of Experimental Equipment

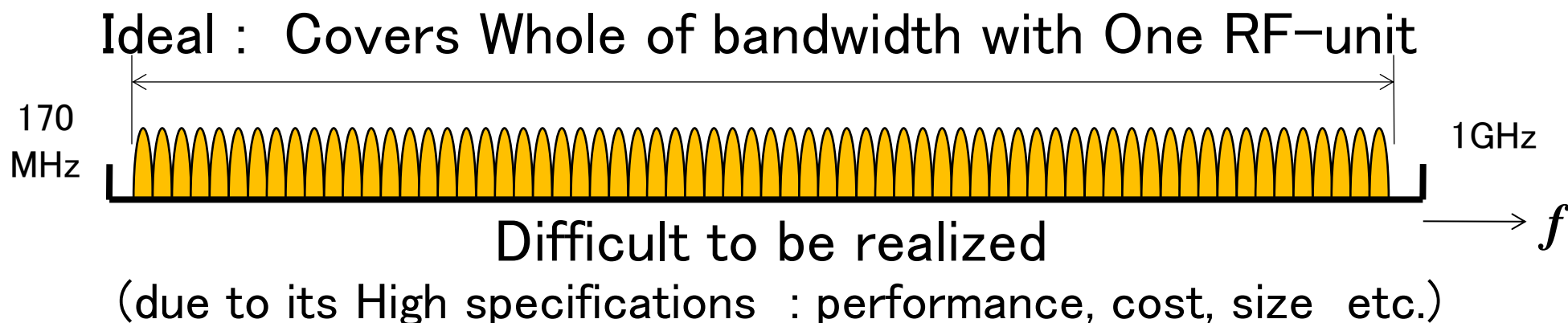


# Block diagram of Experimental Equipment (downlink)



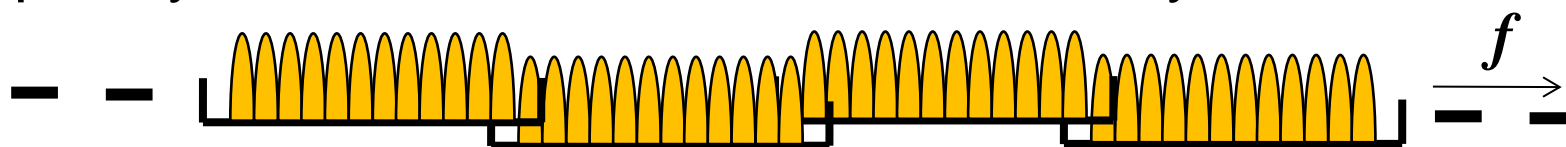


# RF circuit structure for wideband



## ◎ Divided Plural RF-units structure

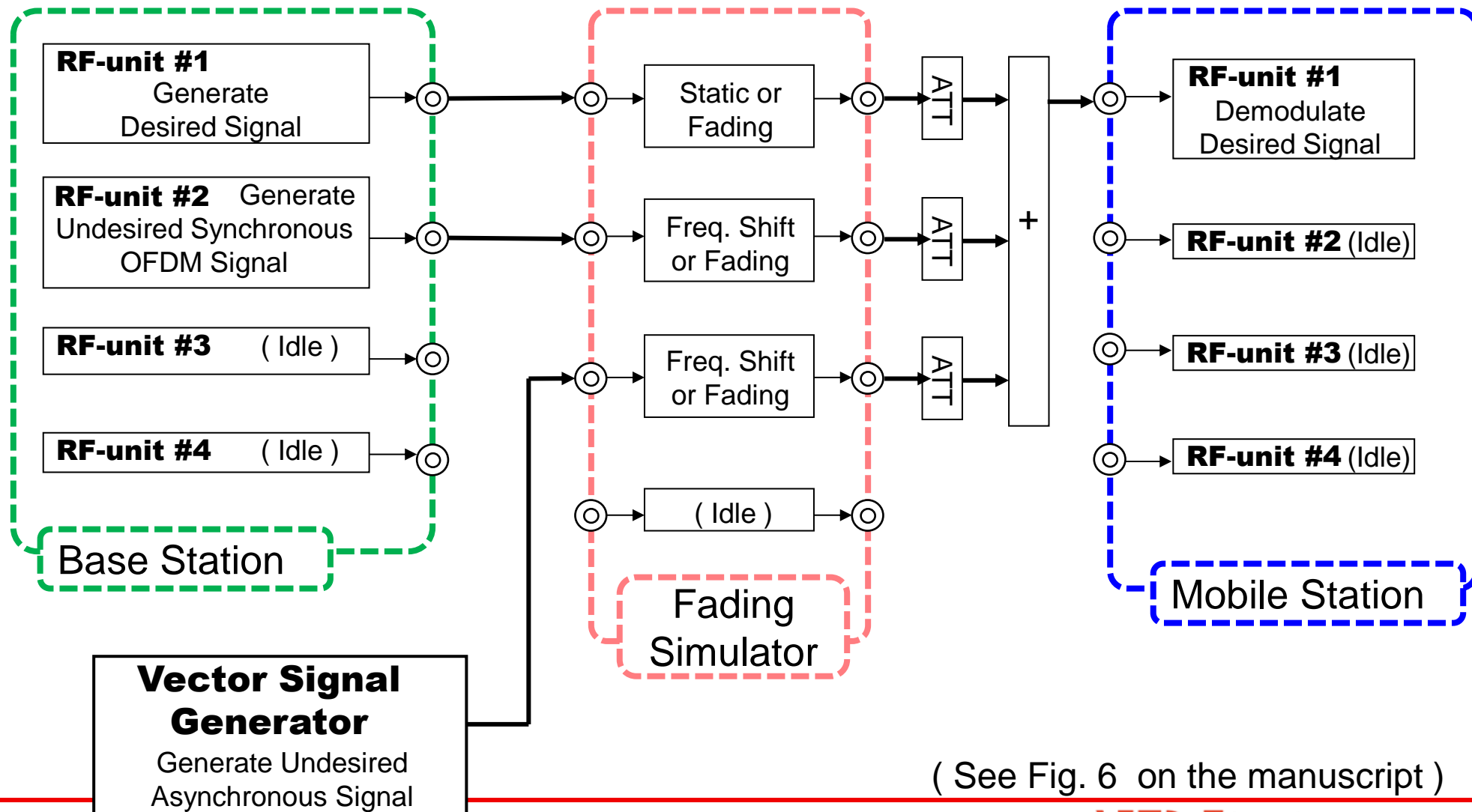
Requirements are relaxed and facilitate the implementation  
Frequency of each RF-unit can be set flexibly



Also Consecutive wide band can be supported



# Experimental Environment



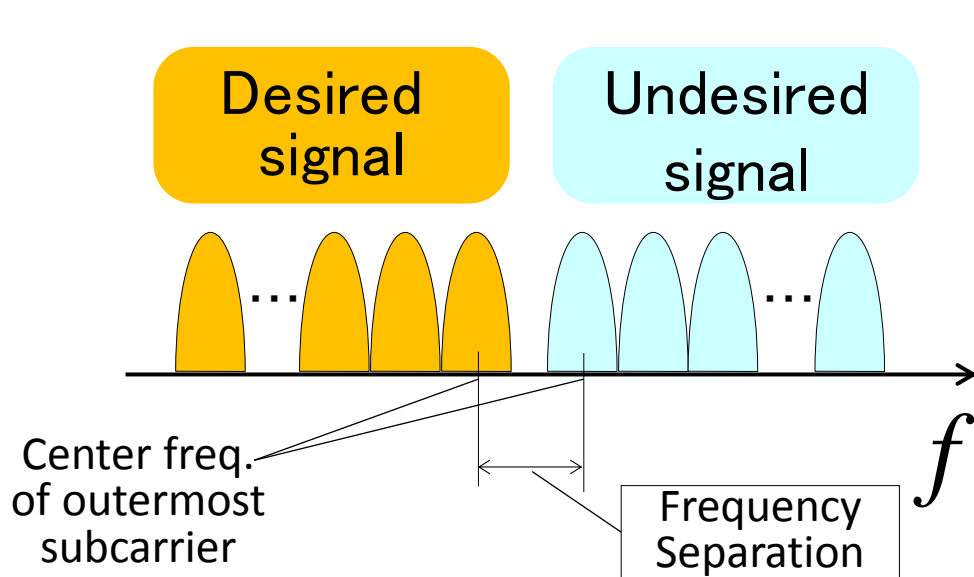
( See Fig. 6 on the manuscript )

# Specification of Signals for Evaluation

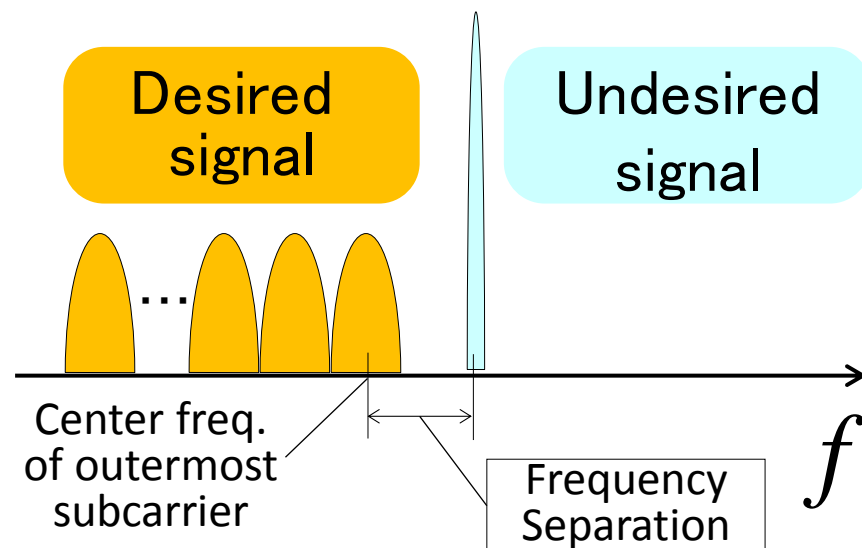
			Signal Format	Band width	Synchro- nization between desired signal	Generated by
Desired Signal	WNC-OFDM		Based on 3GPP- LTE Rel.8 downlink, 15kHz SC spacing, QPSK, No FEC,	9MHz (600 SCs)	-	WNC-OFDM Equipment RF-unit #1
Undesired Signal	OFDM	Synchro nous			Synchronous	WNC-OFDM Equipment RF-unit #2
		Asynchro nous			Asynchronous (different symbol length and timing)	Vector signal generator
	CW				Continuous wave	

( See TABLE 1 on the manuscript )

# Definition of frequency separation in evaluation



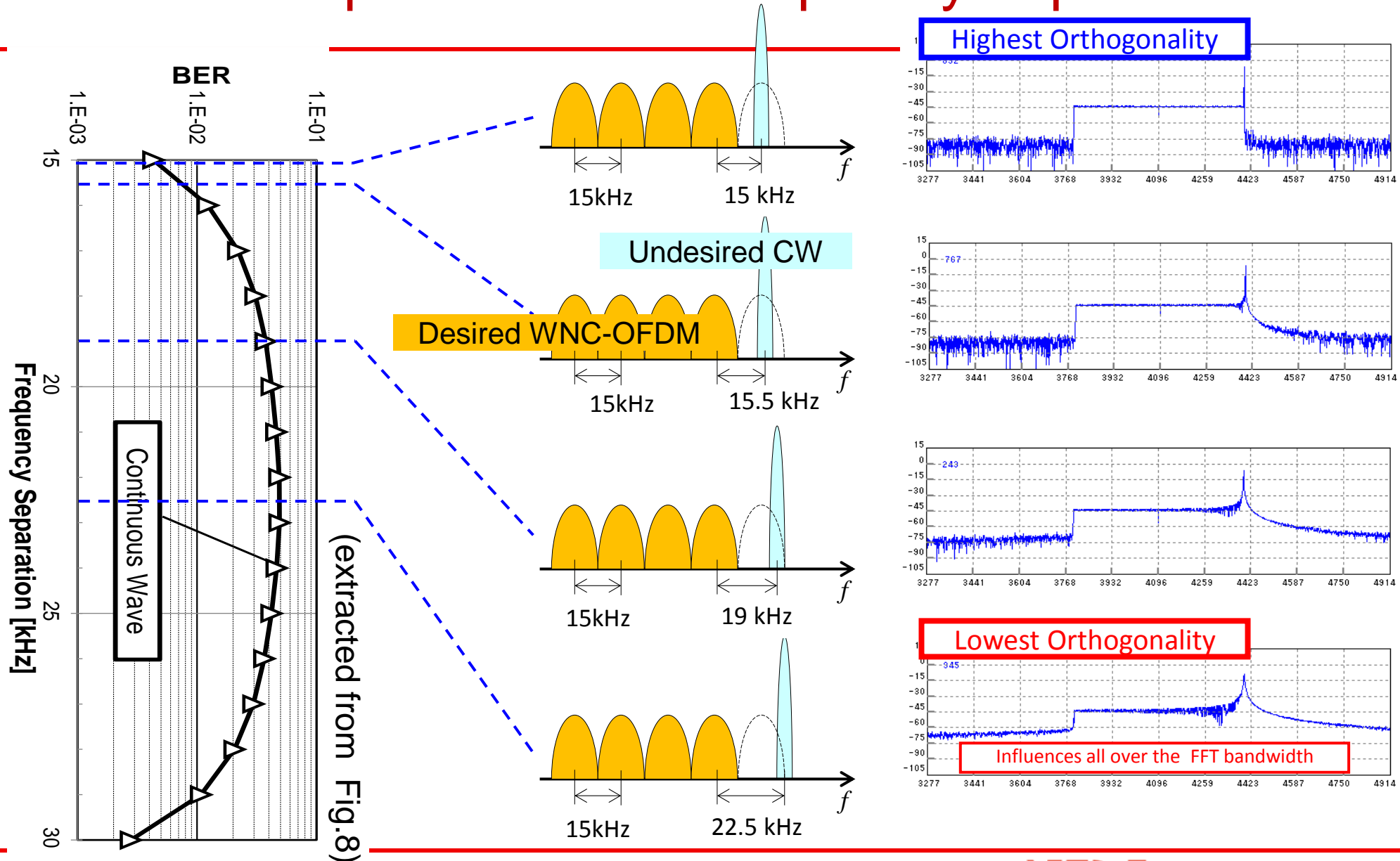
(a) Case of OFDM signal



(b) Case of continuous wave

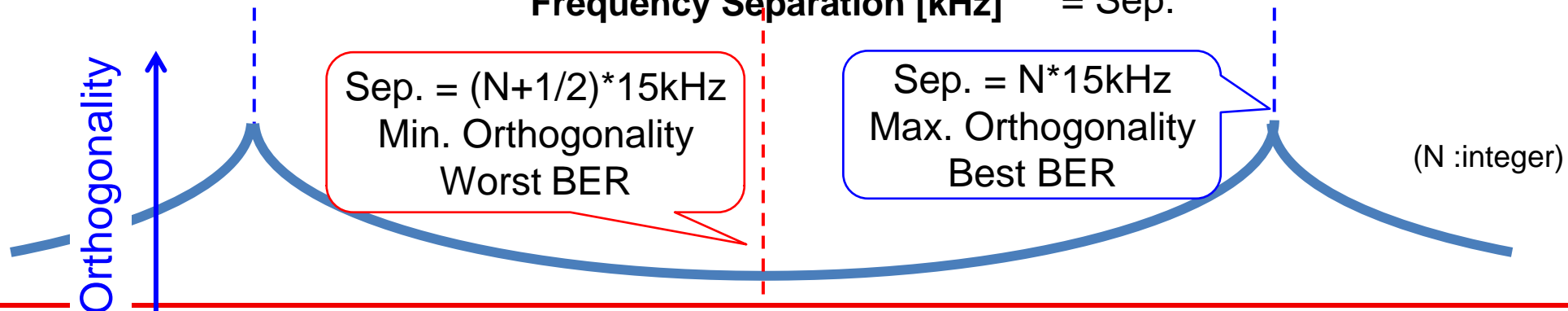
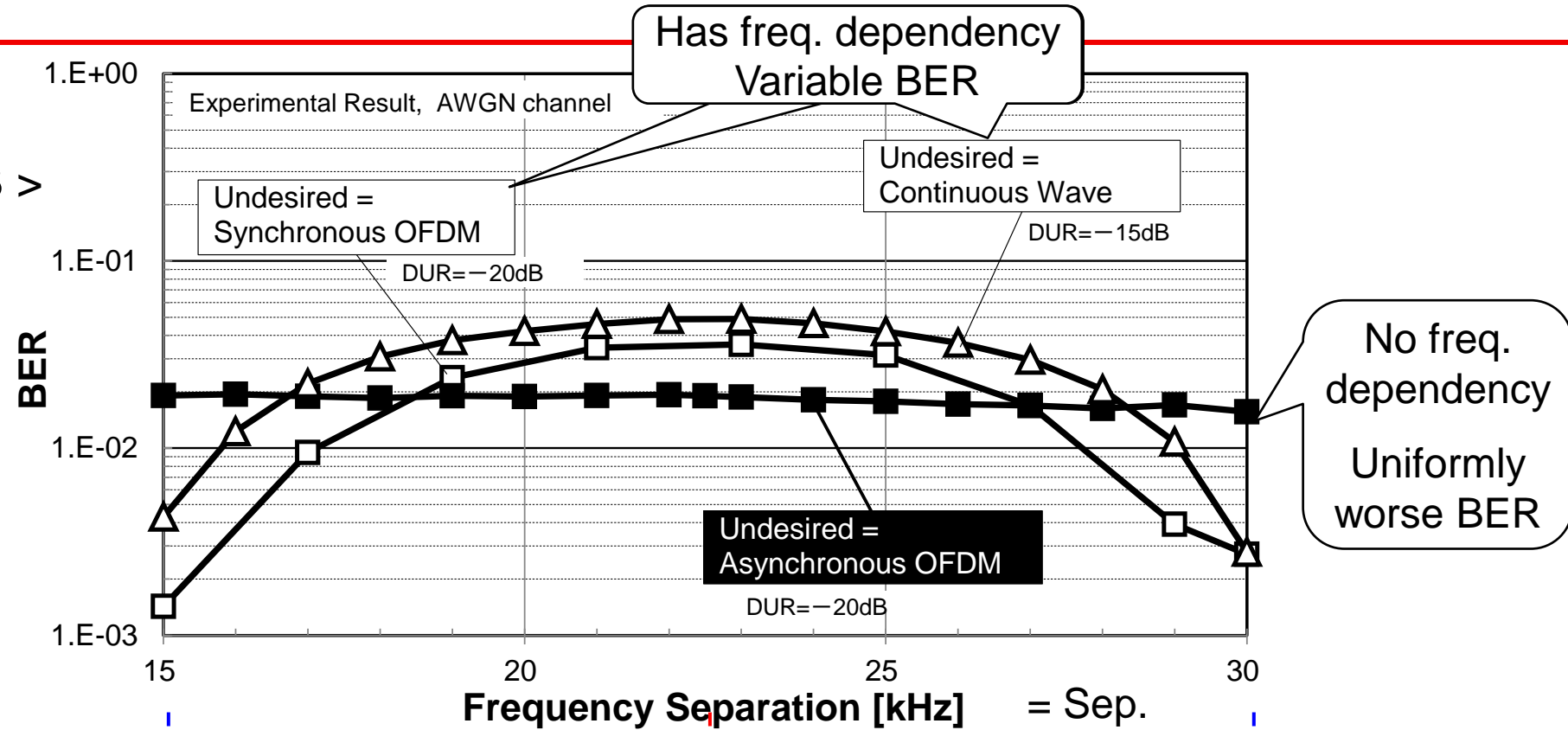
( See Fig. 7 on the manuscript )

# 4.1. BER dependence on frequency separation



# 4.1. BER dependence on frequency separation

< Fig.8 >



## 4.2. BER vs. DUR with undesired synch. OFDM

Experimental Result

&

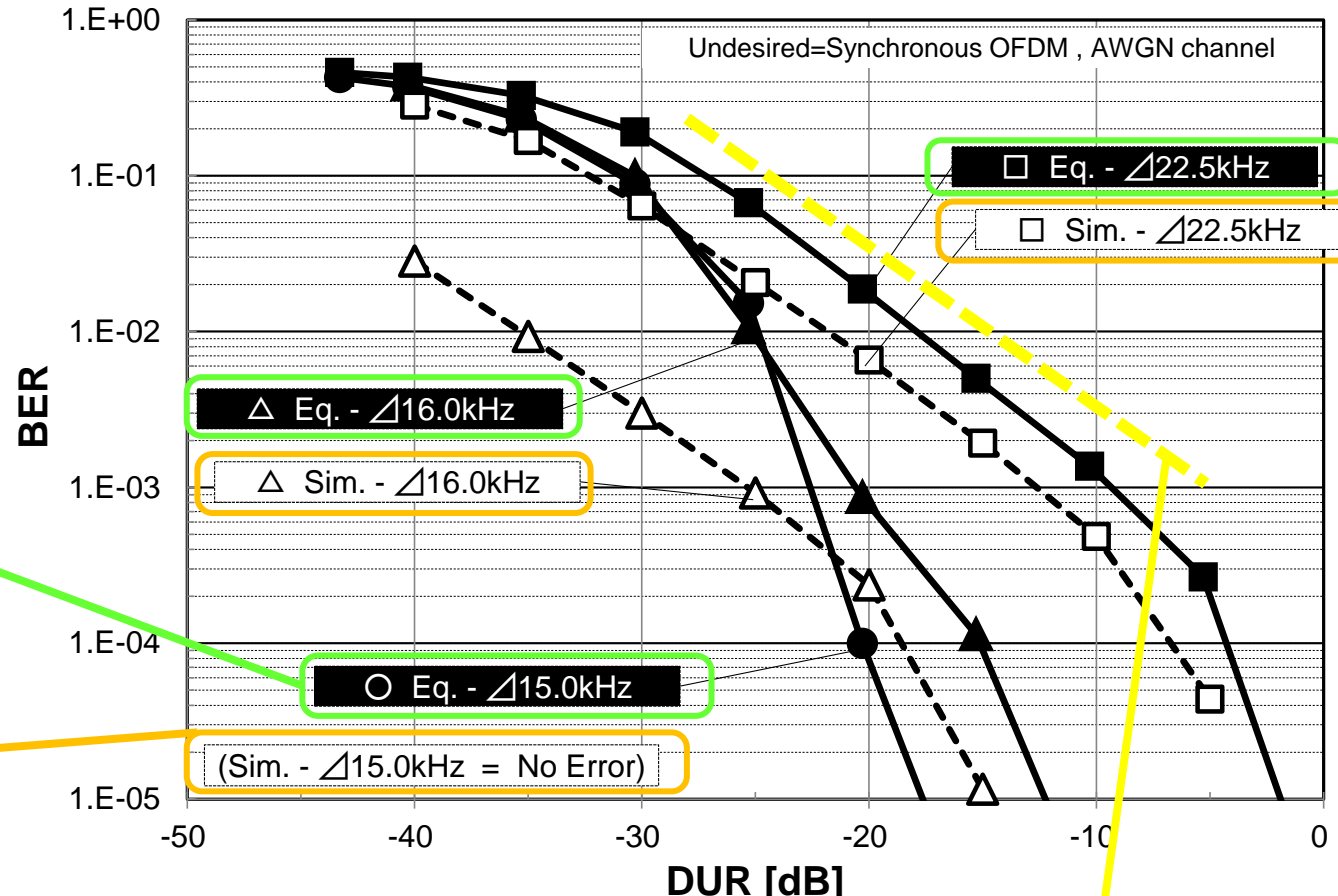
Simulation Result w/o A/D

< Fig.9 >

When  $\Delta$ (freq. separation)  
=15.0kHz, No Error  
occurs theoretically.

Error occurs  
caused by A/D saturation  
or freq. error

No Error  
as theory



- Straight Shaped Graph  
BER x10 / DUR -10dB
- Rapidly fadeout @ <1e-3

Different from usual  
Gaussian interfered  
environment

## 4.2. BER vs. DUR with undesired synch. OFDM

Experimental Result

&

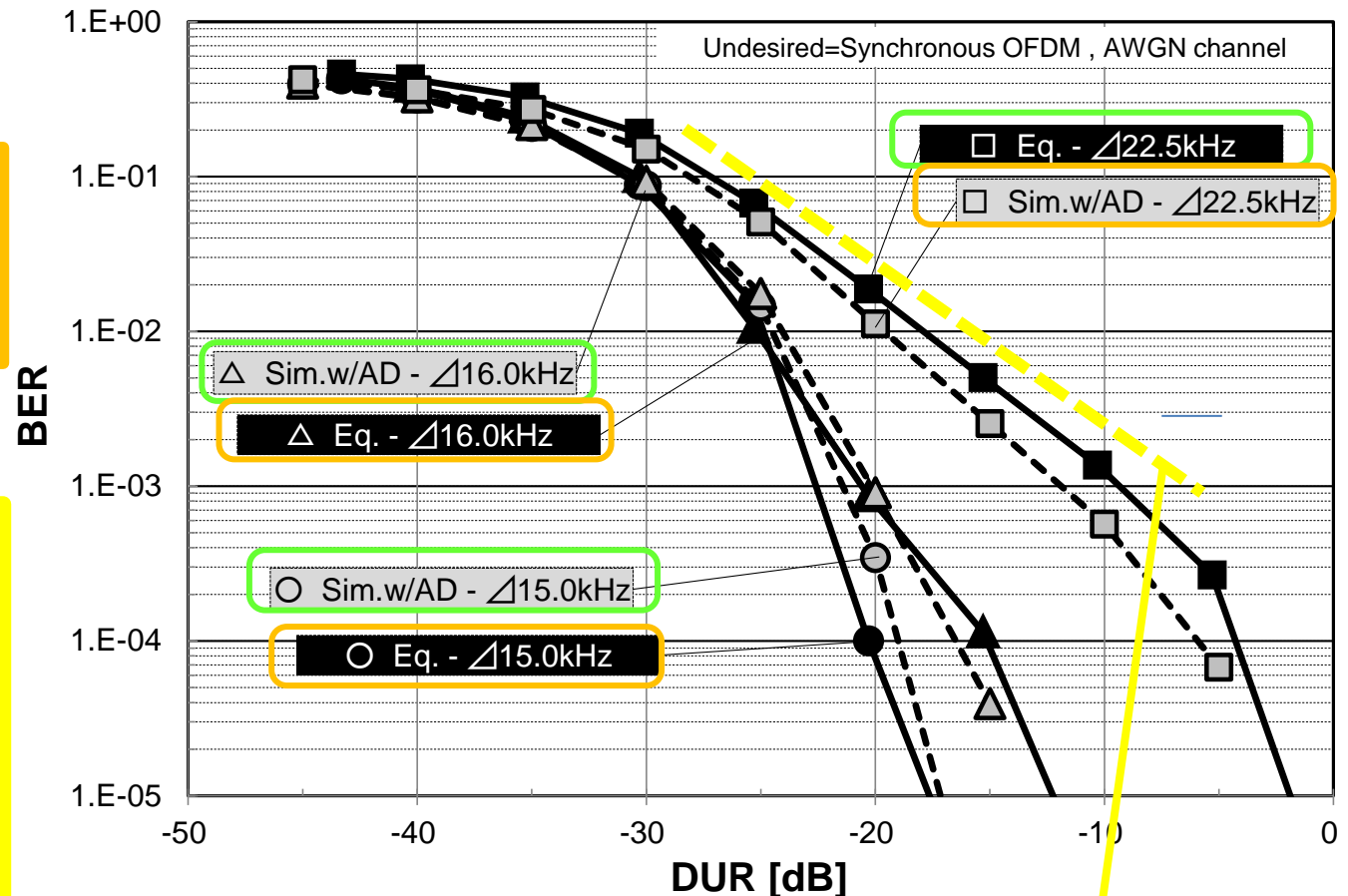
Simulation Result **w/ A/D**

< Fig.10 >

Experimental Result  
and Simulation Result  
become very CLOSE



Confirmed that the  
dominant cause of the  
performance difference  
between **Exp.** and **Sim.**  
is **quantization noise** in  
**A/D** converter.



- Straight Shaped Graph  
BER x10 / DUR -10dB
- Rapidly fadeout @ <1e-3



## 4.3. BER vs DUR with undesired CW

Experimental Result

&

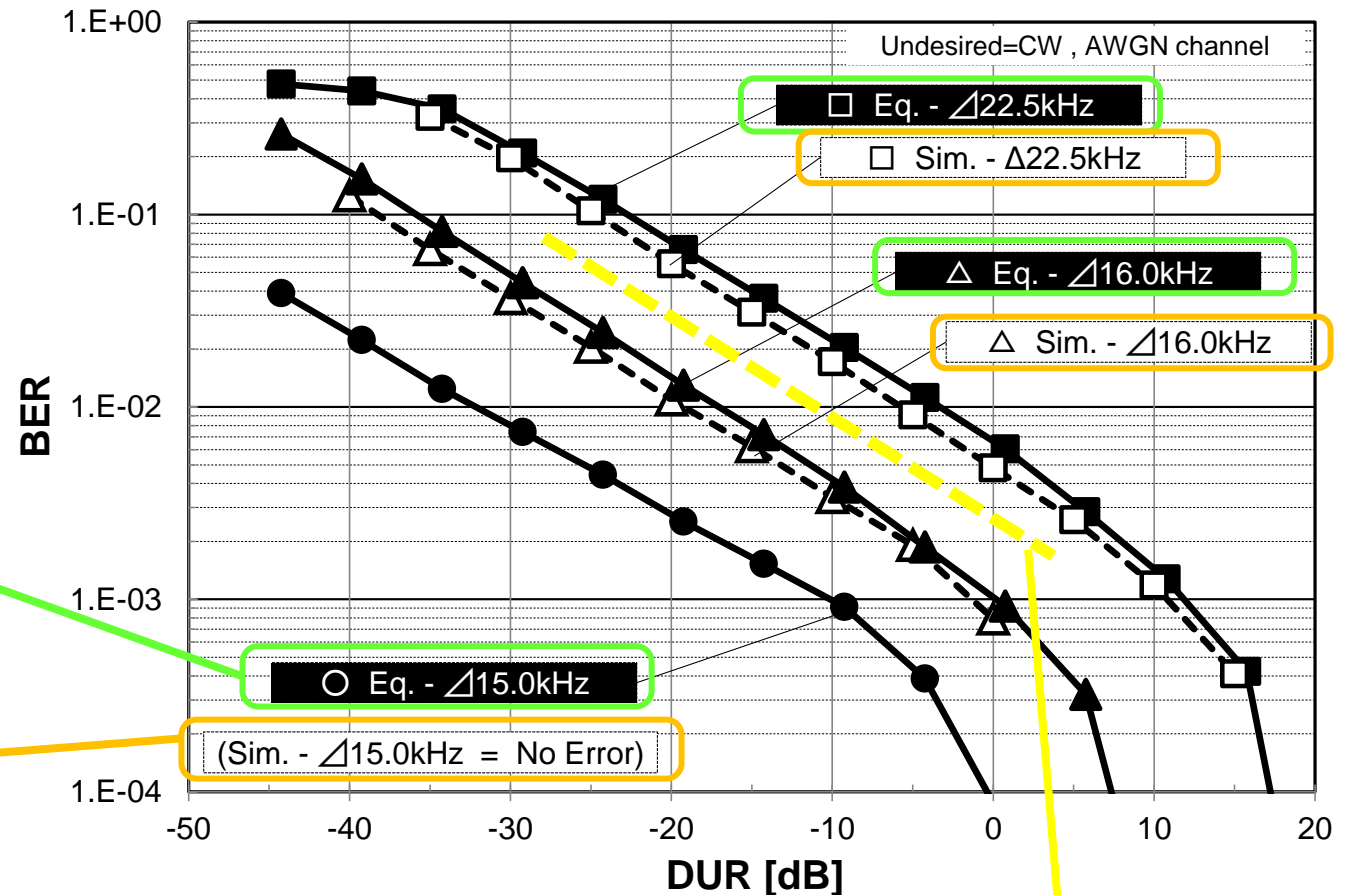
Simulation Result w/o A/D

< Fig.11 >

When  $\Delta$ (freq. separation)  
=15.0kHz, No Error  
occurs theoretically.

Error occurs  
caused by A/D saturation  
or freq. error

No Error  
as theory



- Straight Shaped Graph  
BER x10 / DUR -20dB
- Rapidly fadeout @ <1e-3

Different from usual  
Gaussian interfered  
environment

## 4.3. BER vs DUR with undesired CW

Experimental Result

&

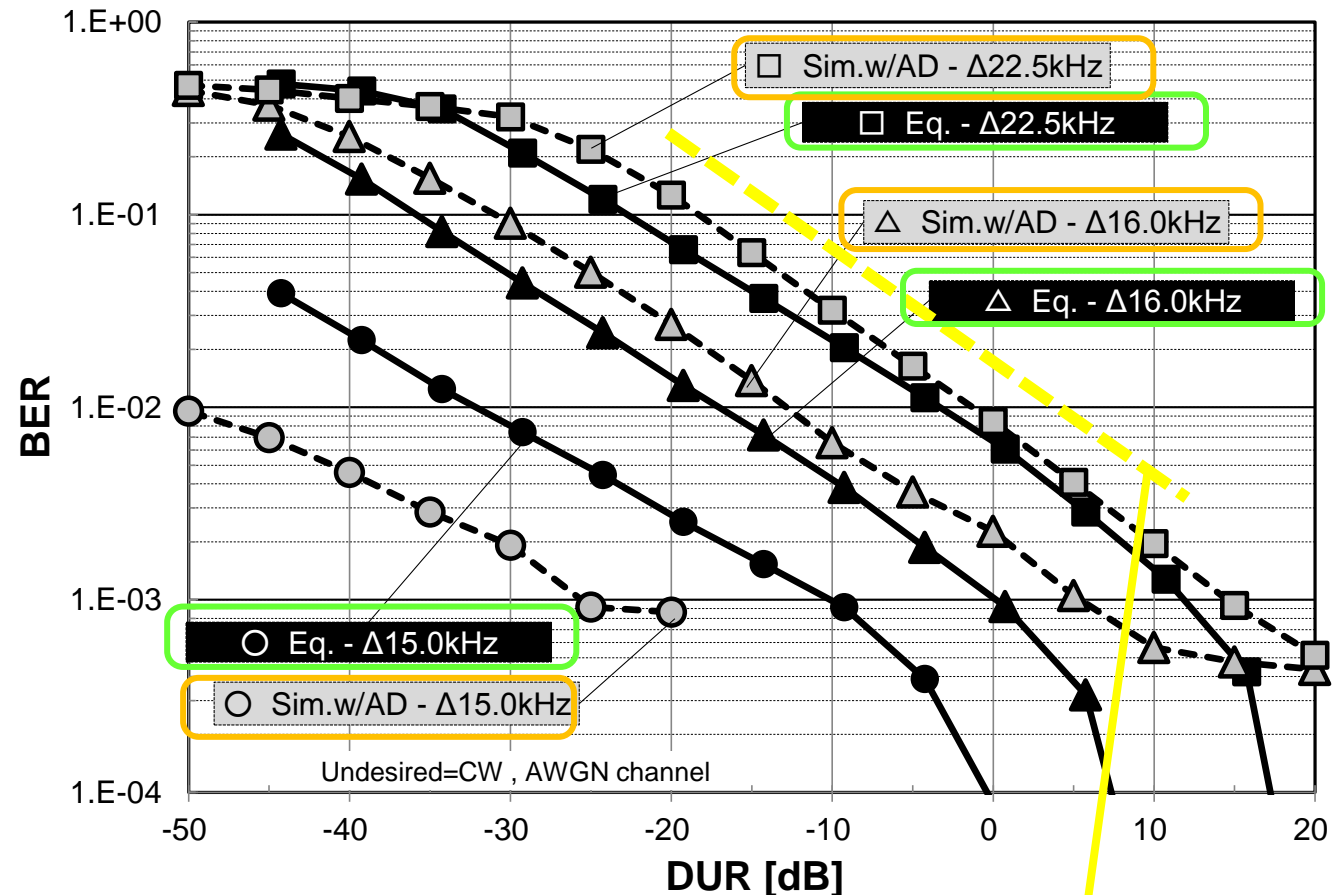
Simulation Result **w/ A/D**

< Fig.12 >

Experimental Result  
and Simulation Result  
get Closer



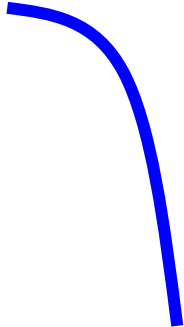
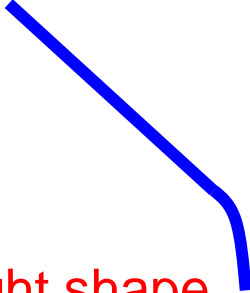
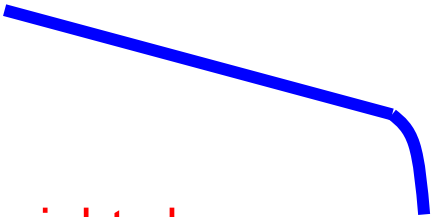
Confirmed that the  
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- Straight Shaped Graph  
BER x10 / DUR -20dB
- Rapidly fadeout @ <1e-3

# 5. Theoretical Analysis

## Summary for characteristics of BER vs DUR graph

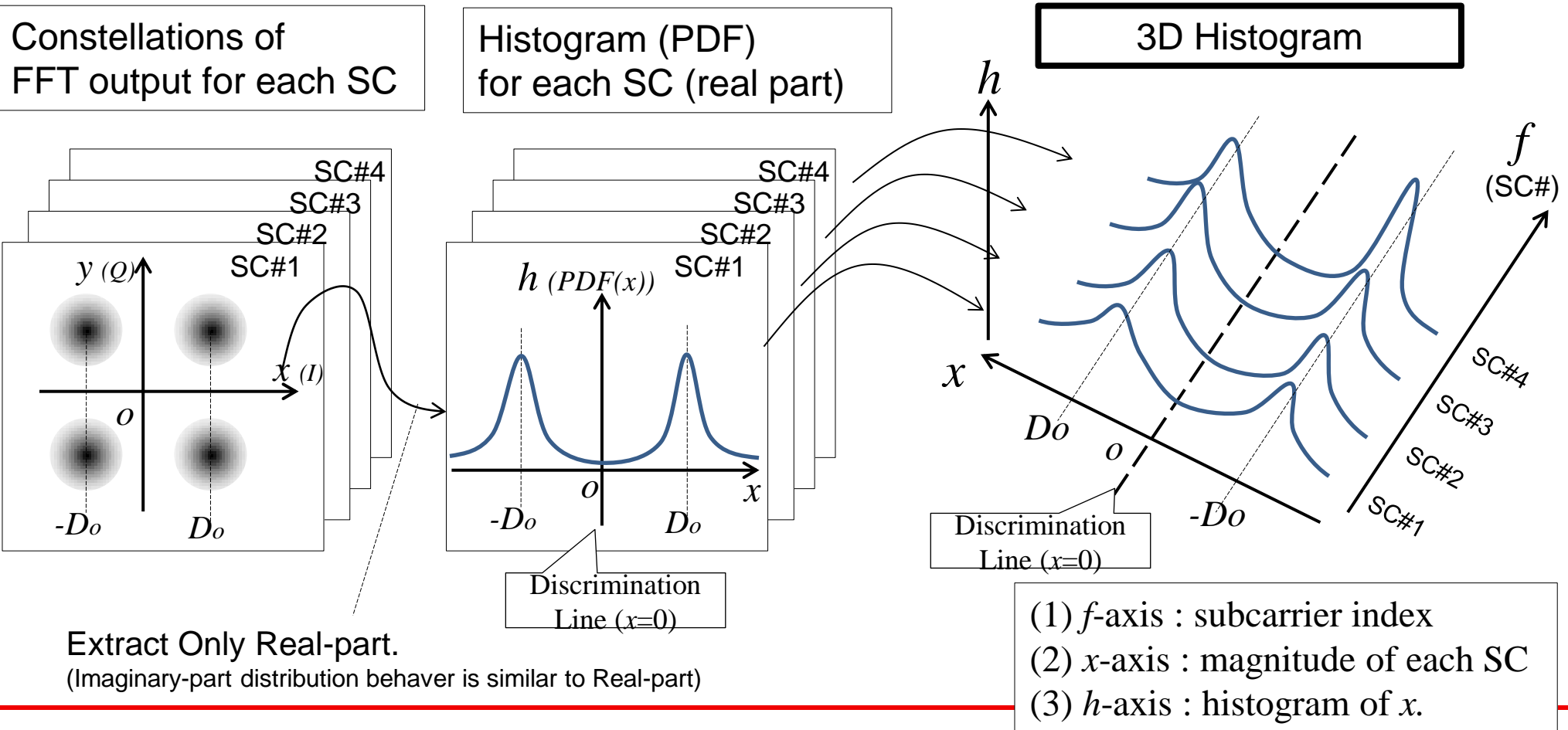
	Gaussian Noise (AWGN)	Synchronous OFDM	Continuous Wave (CW)
Shape of graph		 -Straight shape -Fade rapidly @ $<1e-3$	 -Straight shape -Fade rapidly @ $<1e-3$
Slope of graph	Denoted by Error Function	Small Slope: BER 10 times / DUR 10dB	Small Slope: BER 10 times / DUR 20dB

It was considered that these differences were caused by **difference of distribution shape** of interference.

In this chapter, the different behavior was **theoretically analyzed** in order to comprehend the characteristics more clearly.

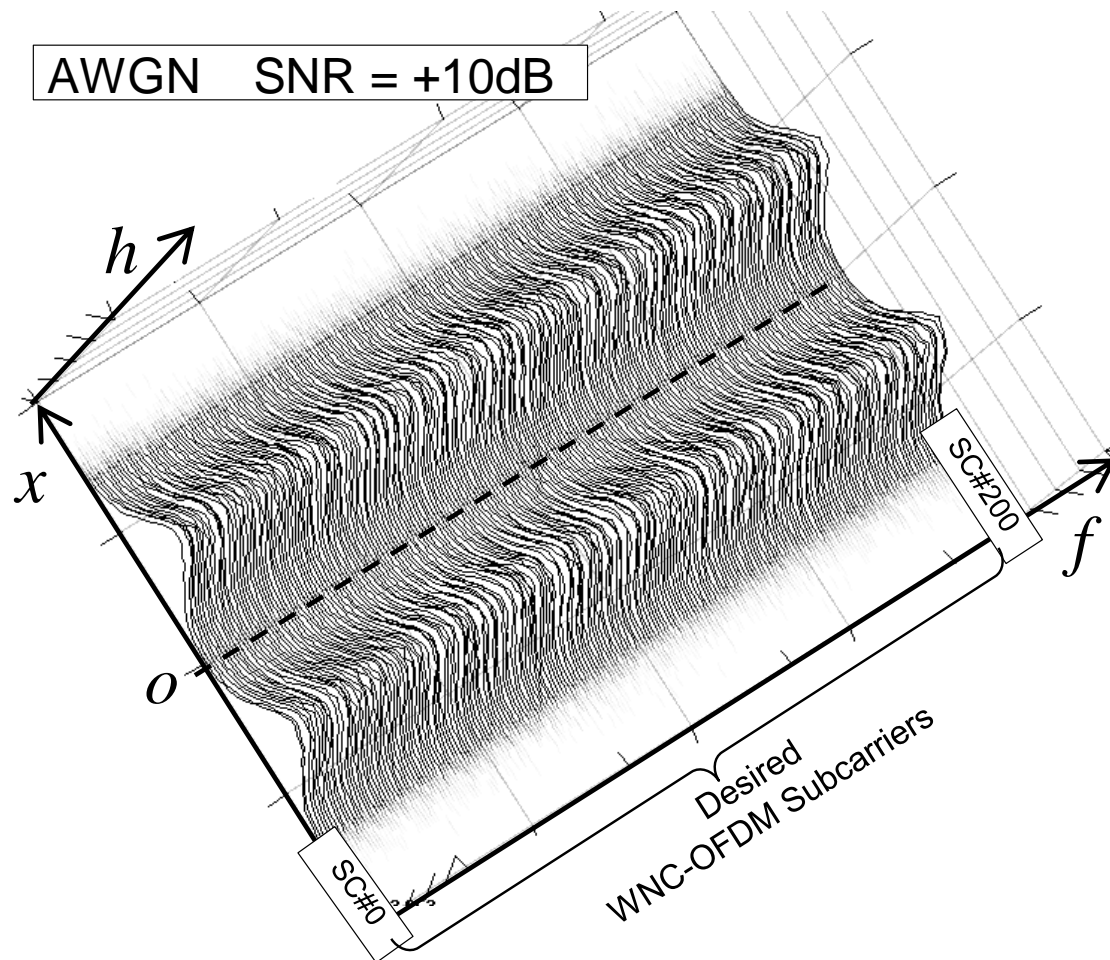
# 5.1. Histogram of Demodulated Signal

For the sake of observation for received signal distribution caused by interferences, **3D Histograms** are drawn by computer simulations.



# Histogram with AWGN

< Fig.14 >

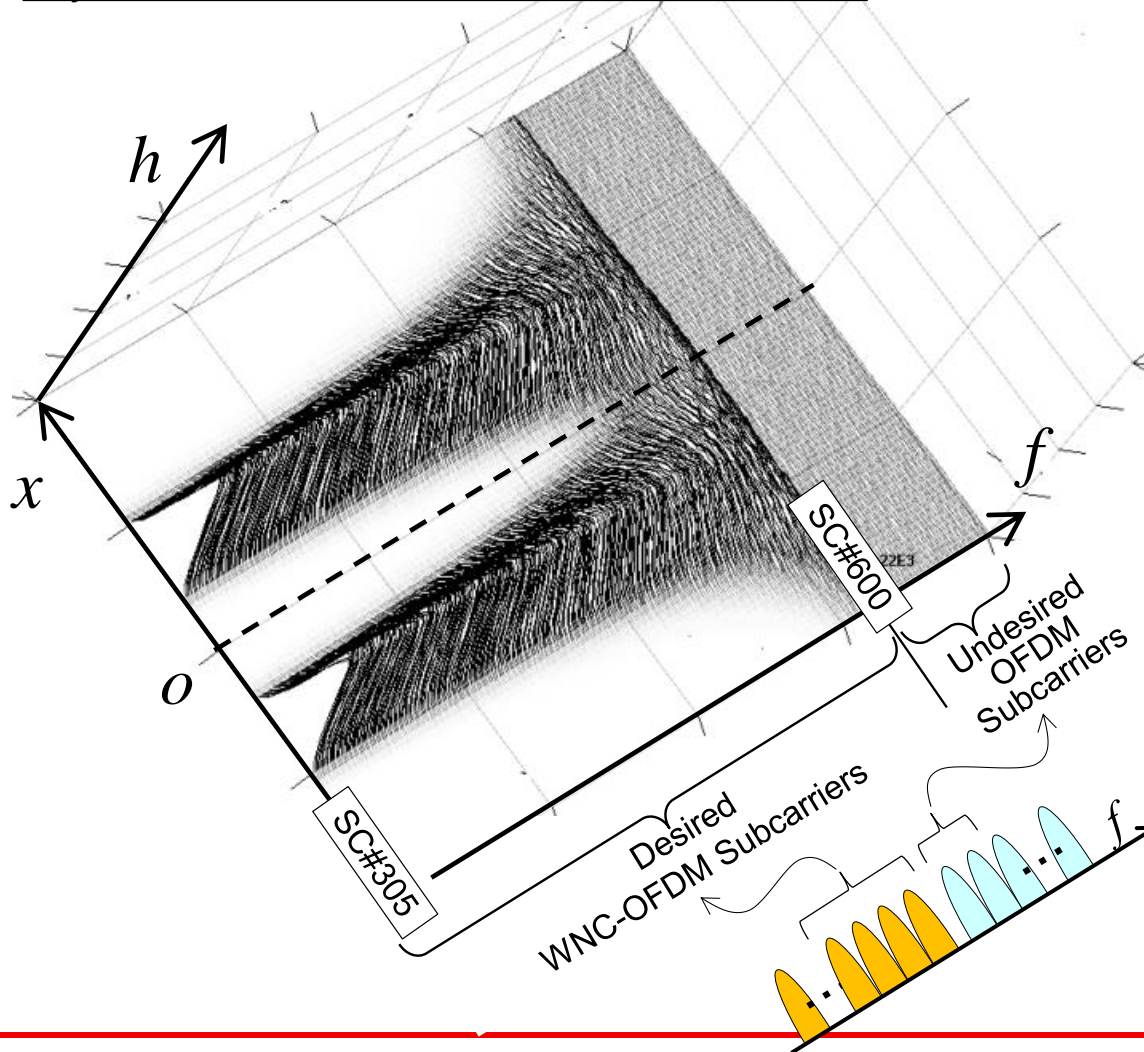


- Gaussian-shape Magnitude Distribution.
- Same Size Distribution for all SC's.

# Histogram with undesired Synchronous OFDM

< Fig.15 >

Synchronous OFDM DUR = -20dB



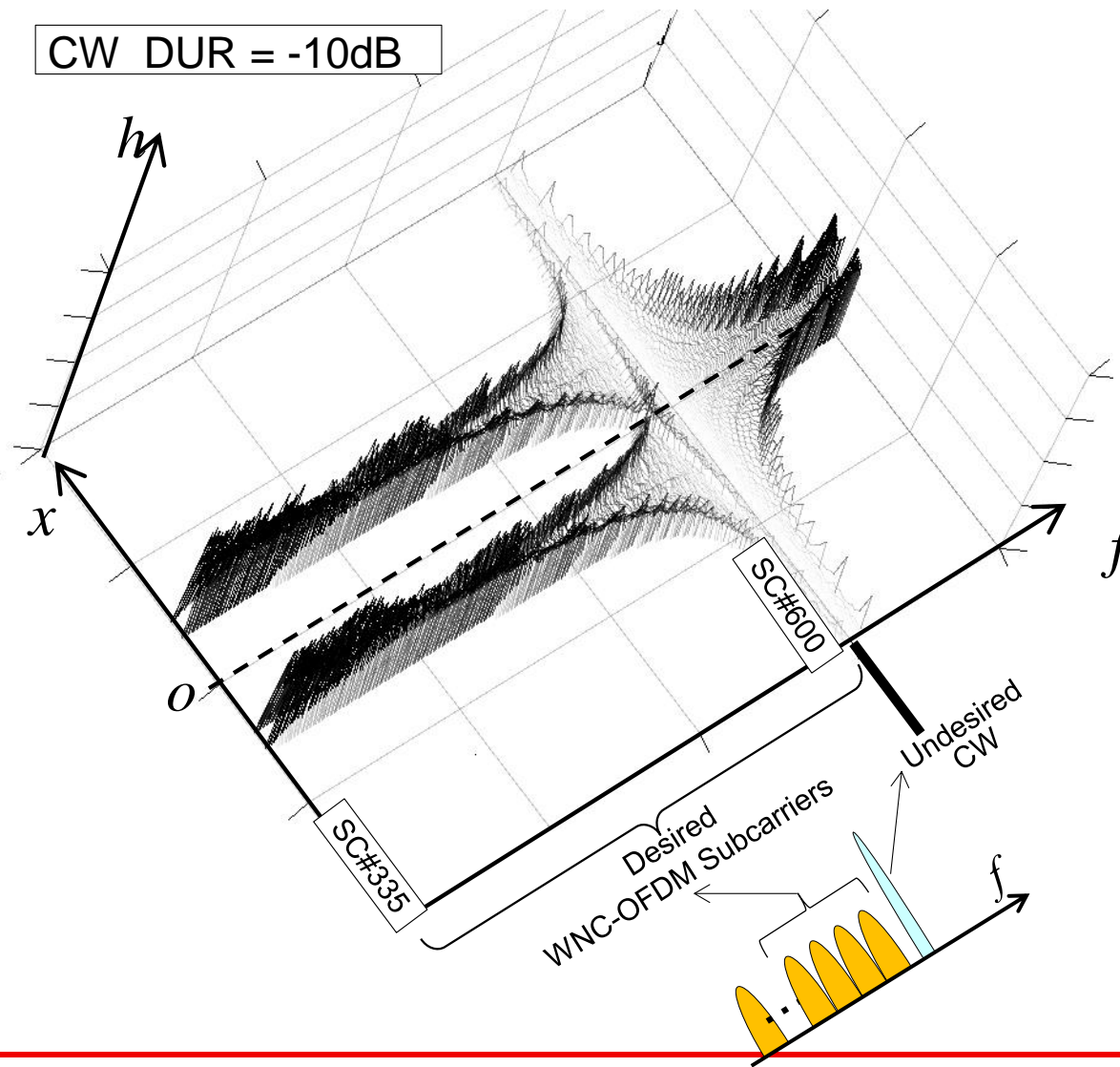
- Magnitude Distributions are **different according to SC index**, (i.e. **frequency**). ( SCs closer to undesired signal are suffered Larger Interference)
- Distribution shape looks similar to Gaussian



# Histogram with undesired CW

< Fig.16 >

CW DUR = -10dB

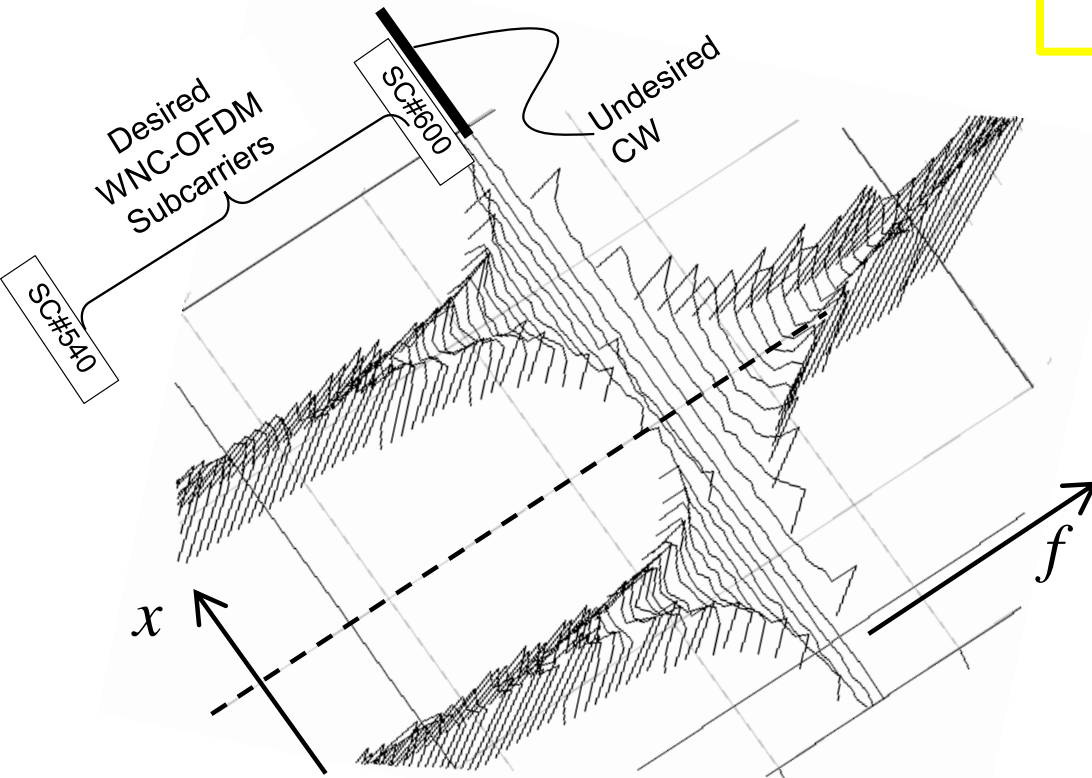


- Magnitude Distributions are **different according to SC index**, (i.e. **frequency**). ( SCs closer to undesired signal are suffered Larger Interference)
- Distribution shape looks like a **letter "M"**.

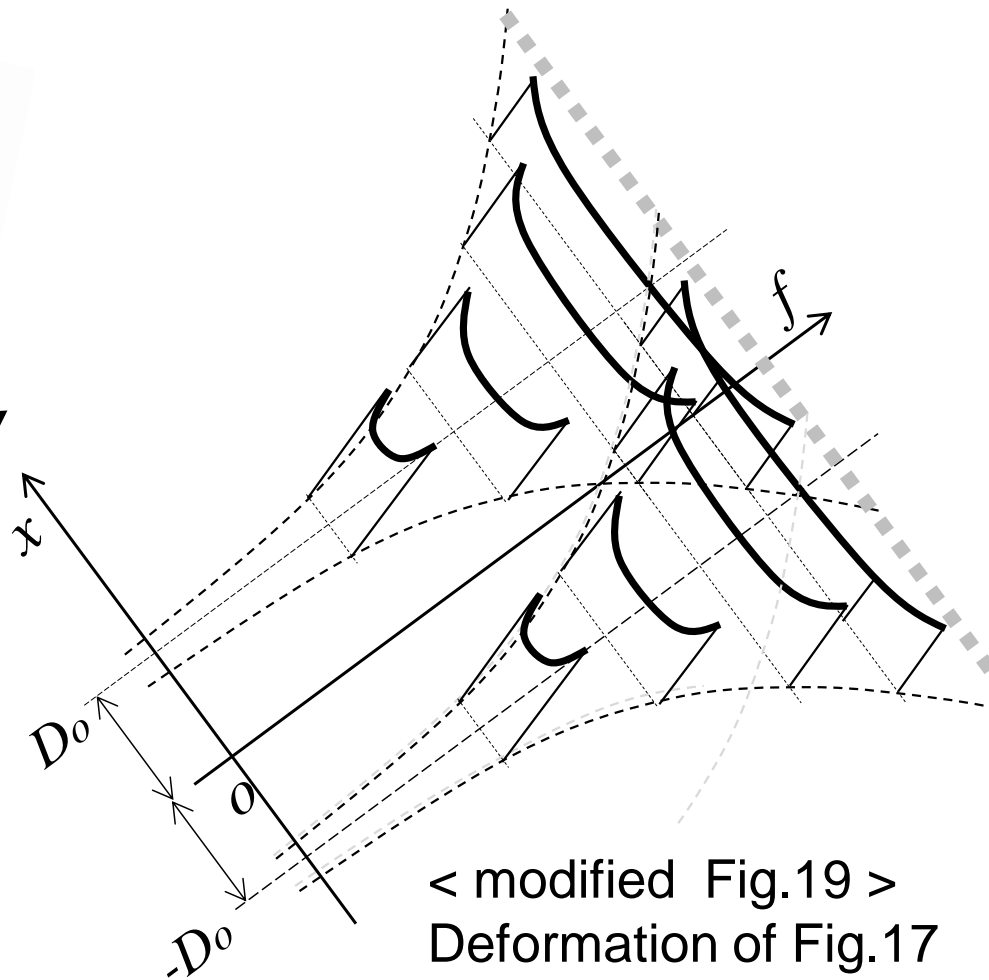


# Histogram with undesired CW (close up)

'M' shaped Distribution

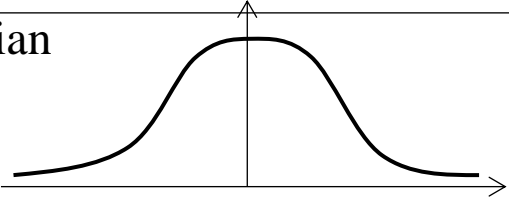
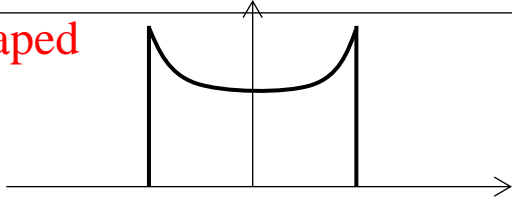
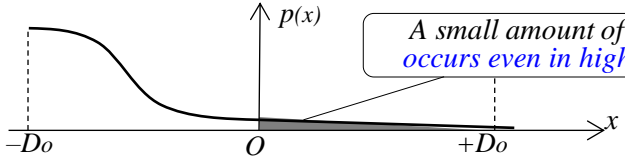
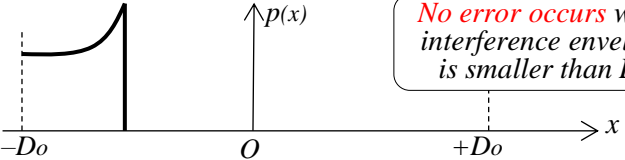
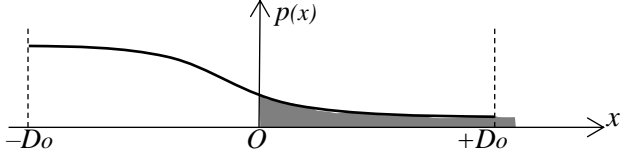
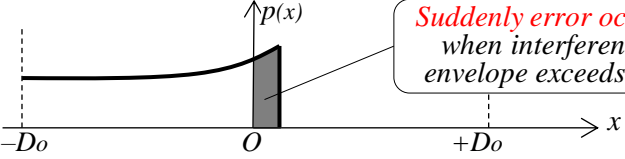
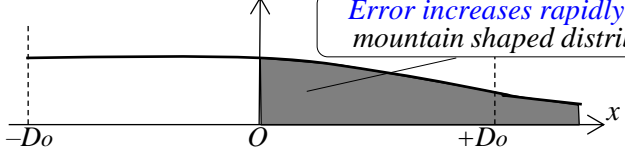
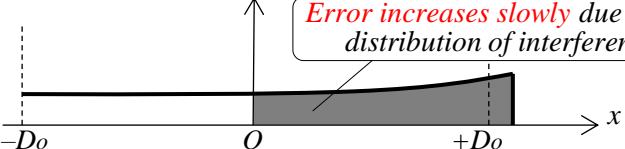


< Fig.17 >  
Close up for Fig.16



# Summary of Histogram Observation

< Extracted from Table 2 >

	Additive White Gaussian Noise (AWGN)	OFDM	Continuous Wave (CW)
Uniformity of Interference	Uniform additive noise - All SCs are always interfered equally	<b>Unbalanced Interference</b> (Larger interference for SCs close to undesired signal) - Number of interfered SCs increases as undesired signal power increases	
Magnitude Distribution of Interference	Gaussian 	Like Gaussian	"M" shaped 
Bit Error Occurrence at One SC of desired signal  High DUR ↑ ↓ Low DUR	 A small amount of error occurs even in high DUR	Bit error rate can be approximated with integration of all interferences from all undesired OFDM SCs. the interference from one undesired SC can be approximated as interference from an undesired CW.	 No error occurs when interference envelope is smaller than $D_o$
			 Suddenly error occurs when interference envelope exceeds $D_o$
	 Error increases rapidly due to mountain shaped distribution		 Error increases slowly due to flat distribution of interference

$x$  = Magnitude of demodulated (FFT output) signal

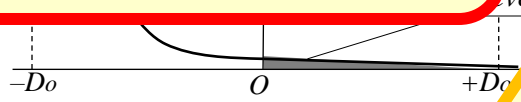
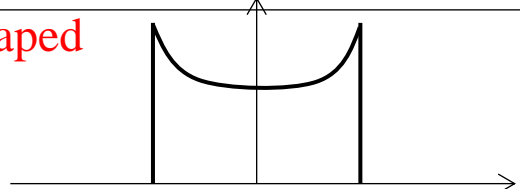
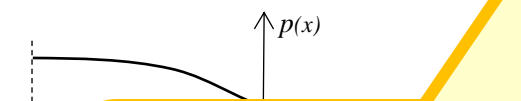
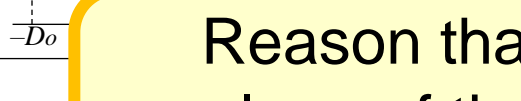
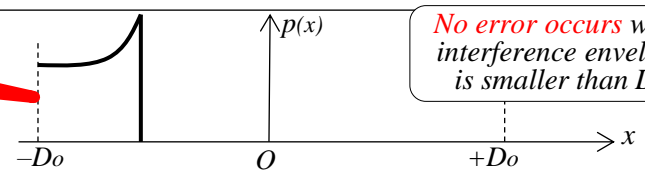

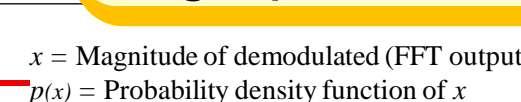
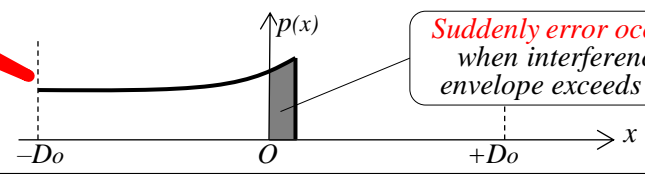

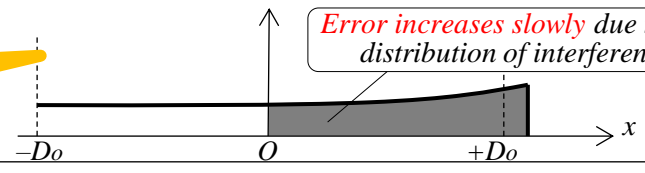
$p(x)$  = Probability density function of  $x$

$D_o$  = Constellation magnitude of desired signal at baseband

$O$  = Origin of  $x$ , and threshold point for sign discrimination

# Summary of Histogram Observation

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Magnitude Distribution of Interference	Gaussian	Like Gaussian	"M" shaped
Bit Error Occurrence at One SC of desired signal	<p><b>Reason that the graph rapidly fadeout @ <math>&lt;1e-3</math></b></p> 		
		<p>Bit error rate can be approximated by integration of all interference from all undesired OFDM SCs. Interference from one undesired SC can be approximated as</p> 	<p>No error occurs when interference envelope is smaller than <math>D_o</math></p> 
			<p>Suddenly error occurs when interference envelope exceeds <math>D_o</math></p> 
			<p>Error increases slowly due to flat distribution of interference</p> 

$x$  = Magnitude of demodulated (FFT output) signal  
 $p(x)$  = Probability density function of  $x$

$D_o$  = Constellation magnitude of desired signal at baseband  
 $O$  = Origin of  $x$ , and threshold point for sign discrimination

## 5.2. Theoretical Analysis for Interference from CW

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It is required to confirm validity for following **Quite Strange** Characteristics in CW interfered environment;

- **"M" shaped** Magnitude Distribution
- **Straight** shaped BER graph

⇒ Theoretical Analysis was executed.

[ Theoretical Analysis for Undesired synchronous OFDM environment ]

⇒ Future Work

Distribution of the interference and BER can be approximated with **Integration** of interferences from **ALL** undesired OFDM subcarriers.

The interference from **ONE** undesired subcarrier can be approximated as interference from **ONE undesired CW**.

## 5.2. Theoretical Analysis for Interference from CW

< 1 > CW component at FFT output

Down-converted CW signal :

$$U(t) = A_u \{ (\cos(2\pi f_\delta t + \varphi_\delta)) + j(\sin(2\pi f_\delta t + \varphi_\delta)) \} \quad (1)$$

n-th SC component at FFT output = Interference Affecting n-th desired subcarrier :

$$F(n) = \int_0^T U(t) \exp(-j2\pi n f_0 t) dt \quad (2)$$

$$= \frac{A_u}{2\pi(f_\delta - n f_0)} \left\{ \begin{array}{l} \sin(2\pi f_\delta N + \varphi_\delta) - \sin \varphi_\delta \\ -j \cos(2\pi f_\delta N + \varphi_\delta) + j \cos \varphi_\delta \end{array} \right\} \quad (6)$$

When  $f_\delta = m f_0$ , zero.  
(Highest Orthogonality)

When  $f_\delta = (m + 1/2) f_0$ , Maximal Magnitude  
(Lowest Orthogonality)

$$F_m = \frac{A_u (-\sin \varphi_\delta + j \cos \varphi_\delta)}{\pi f_0 (m + \frac{1}{2} - n)} \quad (7)$$

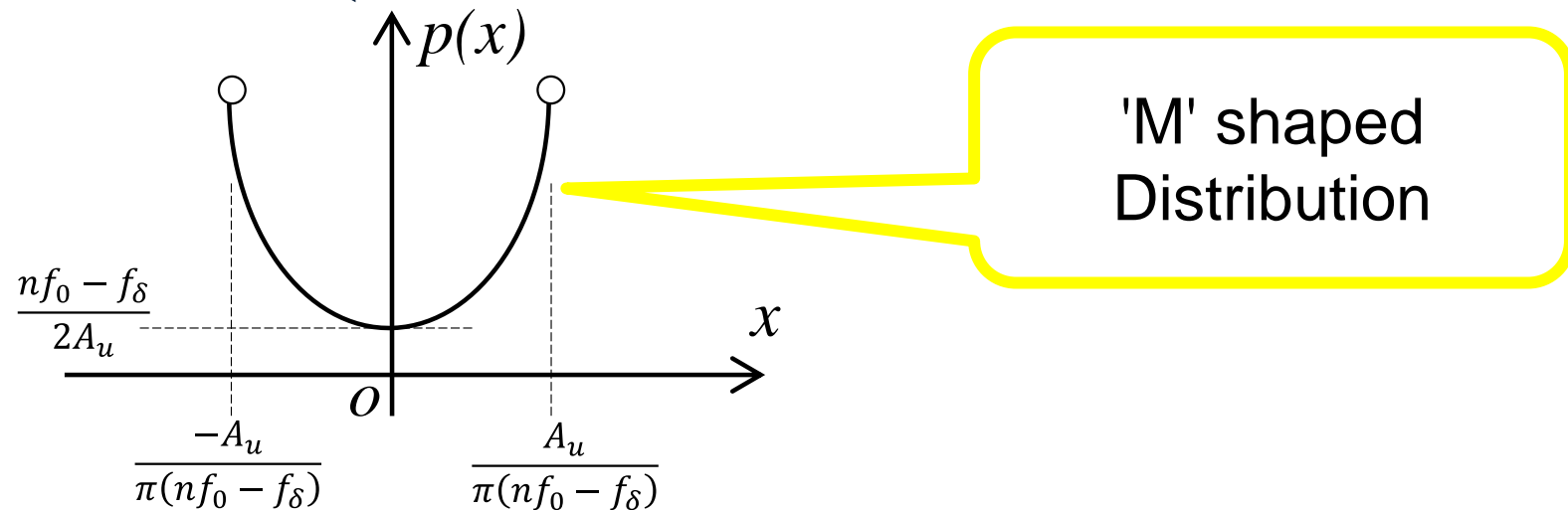
( $m = \text{integer}$ )

## 5.2. Theoretical Analysis for Interference from CW

### < 2 > Probability Density Function (PDF) of Interference component

$$q(S) = \frac{nf_0 - f_\delta}{2A_u} \frac{1}{\sqrt{1 - \left(\frac{\pi(nf_0 - f_\delta)}{A_u} S\right)^2}} \quad (10)$$

$$\frac{-A_u}{\pi(nf_0 - f_\delta)} < S < \frac{A_u}{\pi(nf_0 - f_\delta)}$$

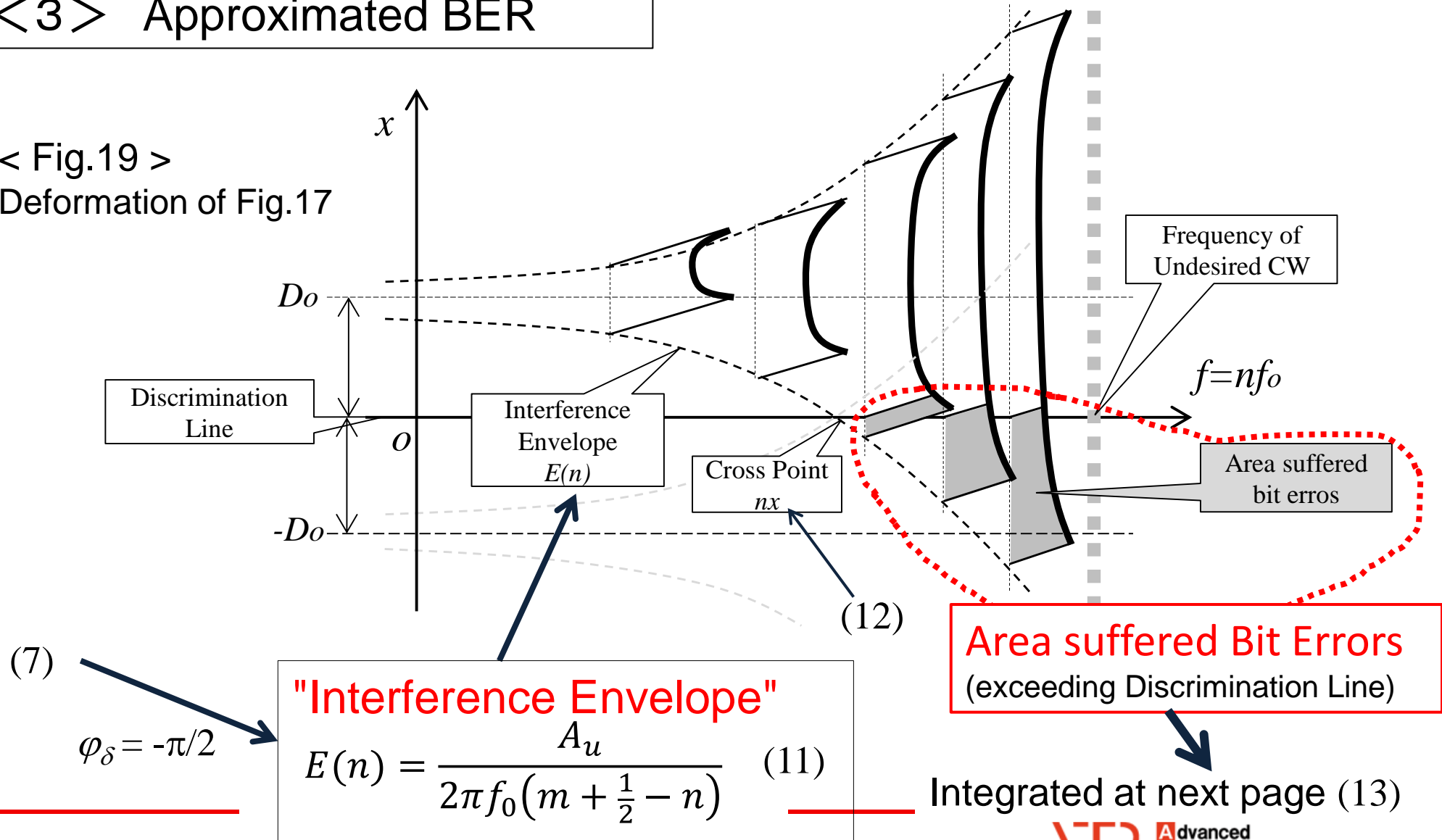


< Fig.19 > PDF of interference from CW

# 5.2. Theoretical Analysis for Interference from CW

## < 3 > Approximated BER

< Fig.19 >  
Deformation of Fig.17





## 5.2. Theoretical Analysis for Interference from CW

### < 3 > Approximated BER

BER is calculated by Sum of (11)= $E(n)$

for area in which  $E(n)$  exceeds the discrimination line.

(PDF of the interference distribution is approximated by rectangular shape)

$$BER = \frac{1}{N} \sum_{n_x}^N (E(n) - D_0) \frac{1}{2E(n)} \approx \left( \frac{A_u}{D_0 \pi f_0} \right) \frac{1}{4N} \quad (13)(16)$$

(16) proves that BER is **Inversely Proportional to DUR**,  
i.e. BER increases 10 times when DUR degrades 20 dB.

(one-tenth in antilogarithm)

Above analysis showed the reason why BER vs DUR graph in undesired CW case had straight shape and small slope (10X BER/20 dB DUR)

# Conclusion

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Influence of interference from other radio system in WNC-OFDM system were evaluated (both experiments and simulation)

BER vs DUR characteristics was **Quite Different** compared to Gaussian noise environment.

- **straight shape**
- **small slope** (10X BER/20 dB DUR : w/ undesired CW)
- **graph rapidly fadeout** @  $<1e-3$ .

These were Theoretically Analyzed and confirmed validity.

These knowledge is valuable for :

- making System Performance Requirement
- Designing a Link Adaptation Algorithm

# Acknowledgment

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This research was performed under research contract of “Research and Development on Wideband Non-Contiguous OFDM”, for the Ministry of Internal Affairs and Communications, Japan

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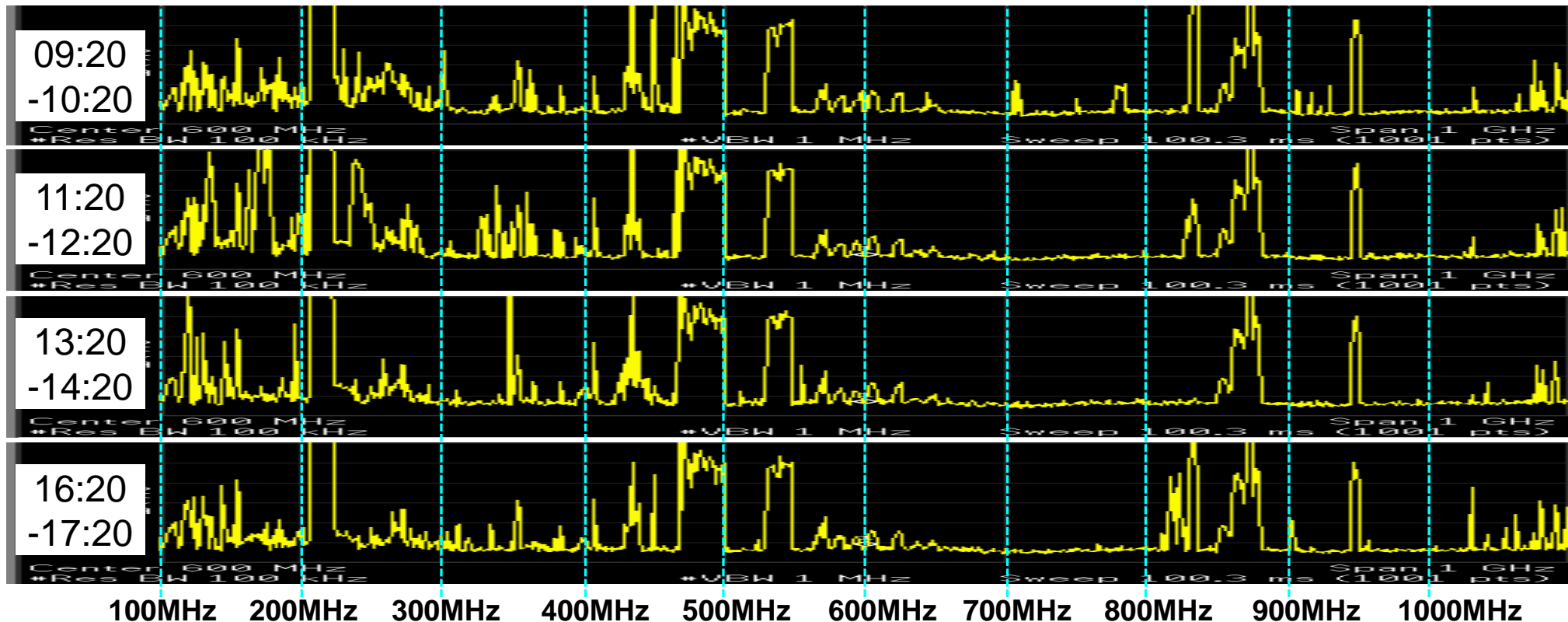
以下 バックアップ

# Observation for Actual Usage of Frequency Bands

Measured at ATR Bld., Kyoto, Japan. 3 Dec. 2012.

Measured w/ biconical antenna & spectrum analyzer, (RBW=100kHz, Max Hold during 1 hour)

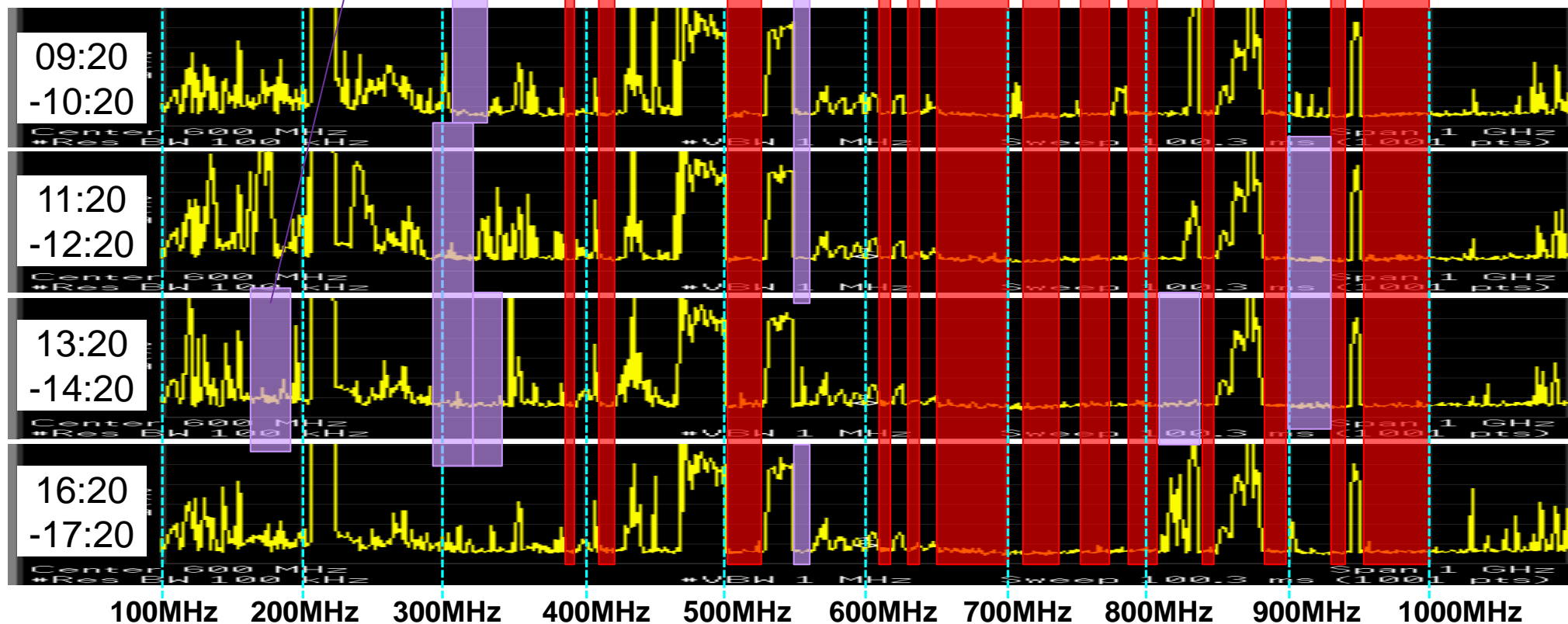
Observed many bands whose **Usage Could Not Be Detected.**  
Observed variation of usage with time passage.



# Observation for Actual Usage of Frequency Bands

Detected No Usage  
in partial interval

Detected No Usage  
throughout the day  
(Max. total 290MHz width)



(Measured at ATR Bld., Kyoto, Japan. 3 Dec. 2012.  
RBW=100kHz, Max Hold during 1 hour.)